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# Qualifying Examination for Supply Learning Support Educators 

## October/November

 2023
## Subject: Mathematics

Date: $\quad$ Thursday $2^{\text {nd }}$ November 2023
Time: (One hour and thirty minutes)

## Instructions to candidates:

- Answer ALL questions.
- Write your answers in the space available on the examination paper.
- Show clearly all the necessary steps, explanations, and construction lines in your working.
- Unless otherwise stated, diagrams are drawn to scale.
- The use of non-programmable scientific calculators with statistical functions and of mathematical instruments is allowed.
- Candidates are allowed to use transparencies for drawing transformations.
- This paper carries a total of 100 marks.

| Question No. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Mark |  |  |  |  |  |  |  |  |  |


| Question No. | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | Total |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Mark |  |  |  |  |  |  |  |  |  |

1. a) Write down a square number that is also an odd number.

Ans: $\qquad$
b) Write down any two prime numbers that lie between 10 and 20.

Ans: $\qquad$
c) Calculate the value of: $7-8 \times(-3)$

Ans: $\qquad$
2. a) Write 0.32 as a fraction in its simplest form.

Ans: $\qquad$
b) Work out $\frac{1}{8}$ of 576 m .

Ans: $\qquad$
c) Simplify $\frac{3^{5} \times 3^{-3}}{3^{6}}$, giving your answer as a fraction.

Ans: $\qquad$
3. Fill in the correct value for each angle:
a) Each angle of an equilateral triangle is equal to $\qquad$ .
b) Opposite angles of a cyclic quadrilateral add up to $\qquad$ -
c) The angle subtended by the diameter of a circle on the circumference is $\qquad$ .
d) The sum of the exterior angles of a polygon is $\qquad$ .
e) One exterior angle of a regular pentagon is $\qquad$ .
f) North-East written as a three-figure bearing is $\qquad$ .
4. On the grid below:
a) Draw the reflection of shape $T$ in the line $L M$. Label the image A.
b) Draw a $90^{\circ}$ anticlockwise rotation of shape T about its vertex N . Label the image B.

5. Petra and Keith are playing a game. They have the following four cards:

| Petra's cards | $\mathbf{1}$ | $\mathbf{3}$ | $\mathbf{5}$ | $\mathbf{7}$ |
| :--- | :--- | :--- | :--- | :--- |
| Keith's cards | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ |

Petra and Keith each pick one of their own cards randomly.
They multiply the numbers on the cards.
a) Complete the probability space below to show all the possible outcomes.

| Petra's Cards |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\times$ | $\mathbf{1}$ | $\mathbf{3}$ | $\mathbf{5}$ | $\mathbf{7}$ |
| Keith's <br> Cards | $\mathbf{2}$ | 1 | 3 |  |  |
|  | $\mathbf{2}$ | 3 | 6 |  |  |
|  | $\mathbf{4}$ | 4 |  |  |  |

b) What is the probability that the answer is an even number?

Ans: $\qquad$
c) What is the probability that the answer is a prime number?

Ans: $\qquad$
(4 marks)
6. Marie uses the following lemon-cake recipe:
a) Write down the ratio of castor sugar : flour in its simplest form.

```
250 grams flour
200 grams castor sugar
130 grams butter
6 eggs
Juice and grated rind of lemon
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Ans: $\qquad$ : $\qquad$
b) Marie bakes four cakes. How much butter does she use?

Ans: $\qquad$
c) Marie spends $€ 19.22$ to buy the ingredients for the four lemon cakes. She divides each cake into 8 equal slices and sells each slice at $€ 1.50$. Work out the profit made on the sale of these four cakes.

Ans: $\qquad$
(4 marks)
7. a) A boat costs $€ 24000$. Calculate the final price of the boat including VAT at $18 \%$.

Ans: $\qquad$
b) Luke buys the boat. He pays a deposit of $€ 12000$, and he pays the rest in 20 equal monthly payments. Work out the amount Luke pays each month.

Ans: $\qquad$
(5 marks)
8. The diagram shows a shed that has the shape of a prism with a cross-section in the form of a trapezium.

a) Calculate the area of the cross-section $A B C D$.

Ans: $\qquad$
b) The volume of the shed is $40.5 \mathrm{~m}^{3}$. Calculate the length CE of the shed.

Ans: $\qquad$
c) Use Pythagoras theorem to calculate the length AD of the sloping roof.

Ans: $\qquad$
9. Angela and Brad start walking from the same point P. Angela walks 50 m on a bearing of $140^{\circ}$. Brad walks 75 m on a bearing of $230^{\circ}$.
a) Draw a scale drawing using 1 cm to represent 10 m showing the new positions of Angela and Brad. Label the positions of Angela and Brad using $A$ and $B$ respectively. Point $P$ is already drawn.

b) Use your scale drawing to find the real distance between Angela and Brad.

Ans: $\qquad$
c) Use trigonometry to calculate $\angle \mathrm{PBA}$. Give your answer correct to 1 decimal place.

Ans: $\qquad$
10. a) The function $f(x)$ is defined by $f(x)=x^{2}-9$. Find $f(-2)$.

Ans: $\qquad$
b) Expand and simplify completely:
$\frac{3(x+3)-(x-3)}{6}$

Ans: $\qquad$
c) The four angles of a quadrilateral measured in degrees are: $x,(2 x-40), 3 x$ and $(x-20)$.

Form an equation and solve it to find the value of $x$.

## Ans:

$\qquad$
d) The side of a square is $(1-3 x) \mathrm{cm}$ long where $x=-2$.

Calculate the perimeter of the square.

Ans: $\qquad$
e) Make $b$ subject of the formula: $a=\frac{b+4}{2}$

Ans: $\qquad$
11. Points $\mathrm{S}, \mathrm{T}, \mathrm{P}$ and Q lie on a pair of parallel lines as shown in the diagram.

SQ and TP intersect each other at R.

a) Show that triangles STR and QPR are similar.
b) $\mathrm{SR}=6.2 \mathrm{~cm}, \mathrm{RQ}=5.9 \mathrm{~cm}$ and $\mathrm{PQ}=10 \mathrm{~cm}$. Calculate the length of ST . Give your answer correct to 1 decimal place.
$\qquad$
12. Listed below are the masses, in grams, of eight new-born kittens:

## $\begin{array}{llllllll}89.4 & 92.6 & 93.1 & 96.2 & 96.8 & 99.7 & 100.2 & 108\end{array}$

Calculate:
a) the median mass;

Ans: $\qquad$
b) the mean mass;

Ans: $\qquad$
c) the range.

Ans: $\qquad$
(6 marks)
13. This pie chart illustrates the number of tourists who visited a summer resort in one of four countries during the year 2022.
a) What percentage of the tourists visited Crete?

Ans: $\qquad$

b) Two thousand tourists visited a resort in Portugal.

Use the information in the pie chart to complete the frequency table below.

| Country | Sicily | Spain | Crete | Portugal |
| :--- | :---: | :---: | :---: | :---: |
| Frequency |  |  |  | 2000 |

14. Three tables and two chairs cost $€ 1900$ while two tables and four chairs cost $€ 1800$.

Let $c$ represent the price in euro of one chair and let $t$ represent the price in euro of one table.
a) Write down two equations in terms of $c$ and $t$.

Ans: $\qquad$

Ans: $\qquad$
b) Solve the simultaneous equations found in part a).

Ans: $c=$ $\qquad$ ; $t=$ $\qquad$
15.a) Draw Design 4 in the pattern shown below:


Design 1
Design 2
Design 3
Design 4
b) Complete the table:

| Design | 1 | 2 | 3 | 4 | 5 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of small squares | 3 | 5 | 7 |  |  |  |

c) Write an expression for the total number of squares in design $n$.

Ans: $\qquad$
16.

a) On the graph above, plot point $\mathrm{Q}(-2,-1)$ and draw the line passing through P and Q .
b) i) What is the gradient of the line $P Q$ ?
ii) What is the $y$-intercept of the line $P Q$ ?

Ans: $\qquad$

Ans: $\qquad$
c) Complete the following table for the equation: $y=x^{2}-2 x-3$

| $x$ | -2 | -1 | 0 | 1 | 2 | 3 | 4 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $x^{2}$ | 4 |  |  |  |  | 9 |  |
| $-2 x$ |  | 2 |  |  | -4 |  |  |
| -3 | -3 | -3 | -3 | -3 | -3 | -3 | -3 |
| $y$ |  |  | -3 |  |  | 0 |  |

d) Draw the graph of $y=x^{2}-2 x-3$ on the grid above.
e) Write down the values of $x$ where the graph of $y=x^{2}-2 x-3$ intersects with line PQ.

Ans: $x=$ $\qquad$ ; $x=$ $\qquad$
17. Points $A, B$ and $C$ lie on the circumference of a circle centre $O . \angle O B C=60^{\circ}$.
$O B$ and $A C$ intersect at $D$ and $\angle A D B=102^{\circ}$.


Calculate the size of the following angles, giving a reason for each of your answers:
a) $\angle \mathrm{ACB}$

Ans: $\qquad$

Reason: $\qquad$
b) $\angle A O B$

Ans: $\qquad$

Reason: $\qquad$
c) $\angle \mathrm{OBA}$

Ans: $\qquad$

Reason: $\qquad$

## End of Paper

